

Hace constar que:

# Andrés Jaramillo Botero

Participó en el 1er Taller Anual: Del Gen al Cultivo como PONENTE -Diseño y Caracterización in-silico de primeros principios de nano-sensores (dispositivos por efecto de campo).

En constancia de lo anterior, se firma en Santiago de Cali a los siete (07) días del mes de diciembre de 2019.

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Andrés Jaramillo Botero Director Científico

Luis Eduardo Tobón Subdirector Fortalecimiento Institucional



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Apoyan:



# Taller anual: Del Gen al Cultivo

P2: Bio-Nanosensores: Prof. Andres Jaramillo Botero y Dr. Juan Manuel Marmolejo (práctica) P3: Modelado Bio-Molecular: Prof. Carlos Arango y prof. Andres Jaramillo Botero

### Parte I

Principios de Simulación Molecular

#### Parte II



# Taller anual: Del Gen al Cultivo

Prof. Andres Jaramillo Botero Dr. Juan Manuel Marmolejo (práctica)

### Taller 2: Diseño de nanosensores para biomarcadores

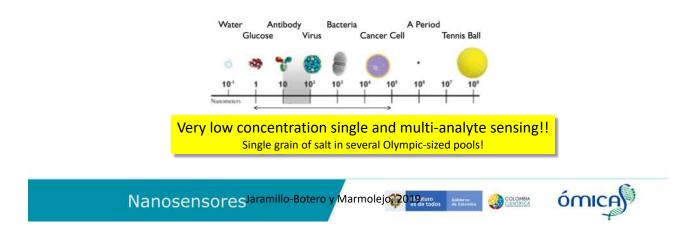
#### Contenido:

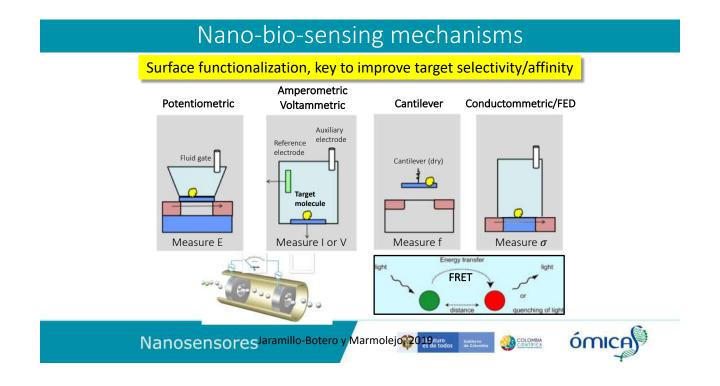
- Fundamentos de la nano-escala
- Estructura electrónica de materiales
- Mecánica y Dinámica Molecular
- Bio-nano-sensores
- Nano-sensores (efecto de campo)
- Transporte electrónico en dispositivos
- Propiedades termodinámicas

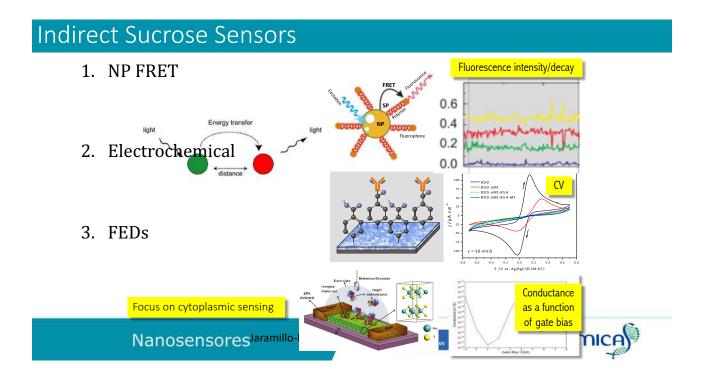
Nanosensores 🛛 🖗 El futuro de Sectores Ómica

Objective

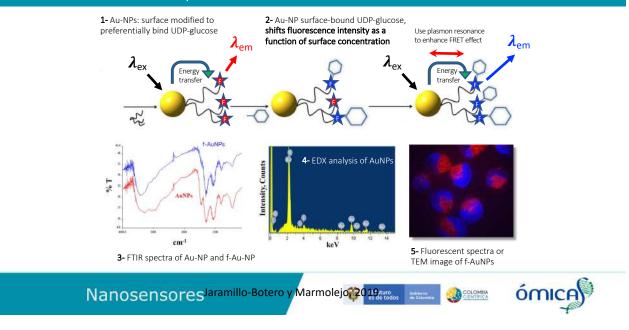
In-silico design, characterization and screening of nano-sensor device architectures for detection of biomarkers at nM-pM/L concentrations (mM/L)



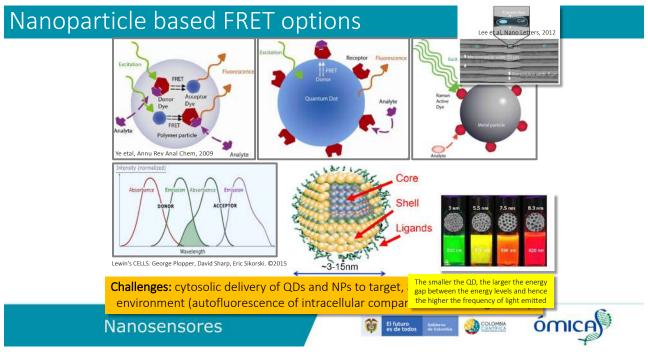


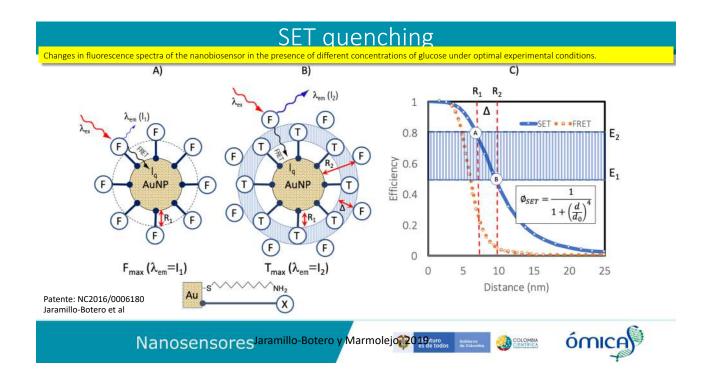


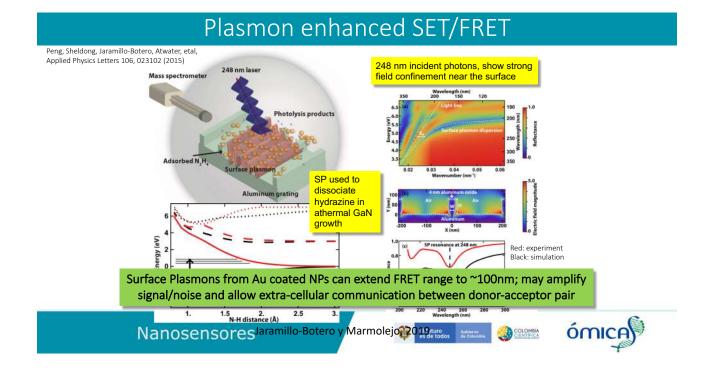
### In-Vivo Gold-nanoparticle-based Sucrose/Starch FRET sensors

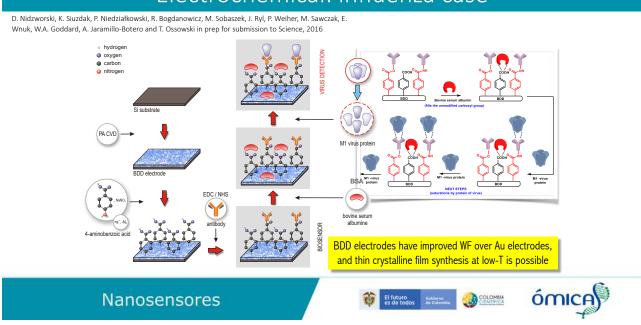


#### Jaramillo-Botero y Marmolejo, 2019







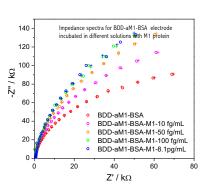


### Electrochemical: influenza case

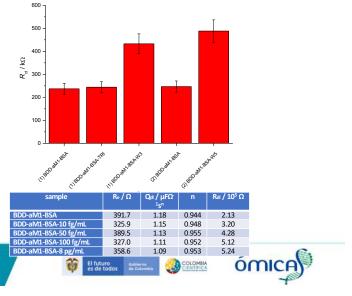
# Electrochemical: results

D. Nidzworski, K. Siuzdak, P. Niedziałkowski, R. Bogdanowicz, M. Sobaszek, J. Ryl, P. Weiher, M. Sawczak, E. Wnuk, W.A. Goddard, A. Jaramillo-Botero and T. Ossowski under submission to Nature Nanotechnology, 2016 100 BDD - BDD-aM1 - BDD-aM1-BSA 75 Соон Соон 50 BDD-aM1-BSA-M1 j/μA cm<sup>-2</sup> 25 -2 -50 -75 -100 v = 50 mV/s4 -0.2 0.0 BSA: Bovine Serum Albumin E /V vs. Ag/AgC I/0.1M K C I 0.8 -0.4 For pristine BDD electrode the difference between oxidation and reduction potential peak equals 0.17 V, whereas when M1 antibody was bound, current decreases and h potential difference grows to 0.36 V. After incubation of BDD-aM1 electrode in BSA or M1 protein solution, no oxidation or reduction peak was observed. Drastic change in CV from efficient blockage of e- transfer between electrode and redox active species 254 256 285 290 Binding Energy / eV 316 400 404 435 Stridling Emergy LeV 834 836 ÓMICA Nanosensores T El futuro es de todos

# Impedance spectra and EEQC



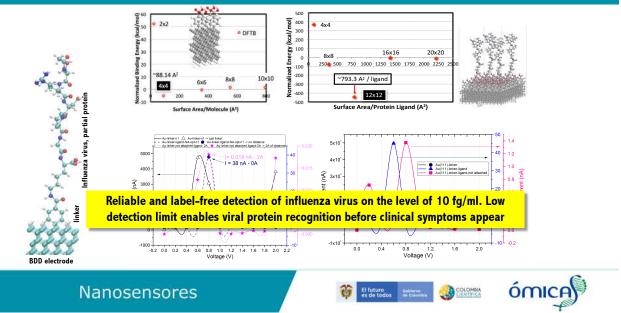
Impedance spectra of BDD-aM1-BSA electrode after incubation with different M1 concentrations recorded in 1 mM K<sub>3</sub>Fe(CN)<sub>6</sub> + 0.1 PBS at  $E_f$  = + 0.13 V vs. Ag/AgCl/0.1M KCl



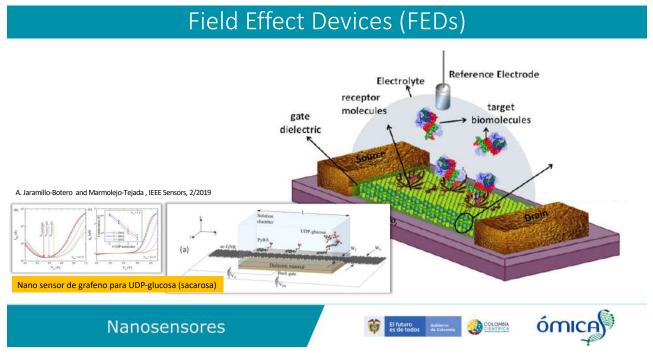
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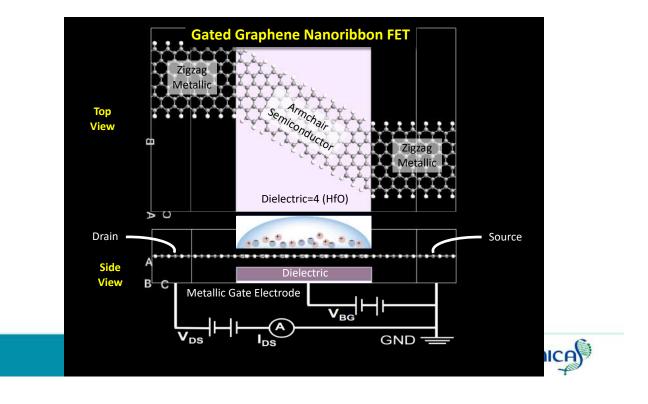
# Surface coverage and IV analysis

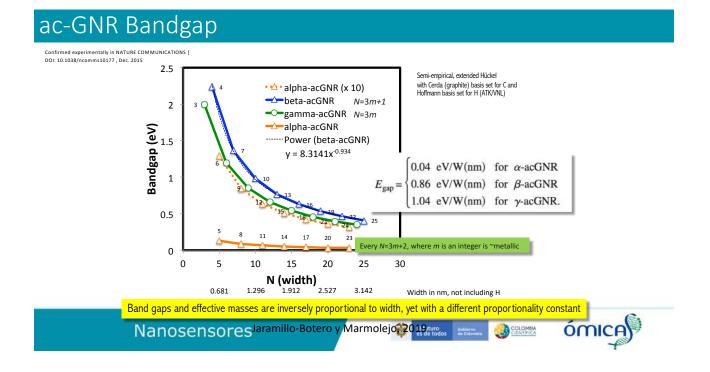
Impedance analyzed on the basis of an electric equivalent circuit (EEQC) using an EIS

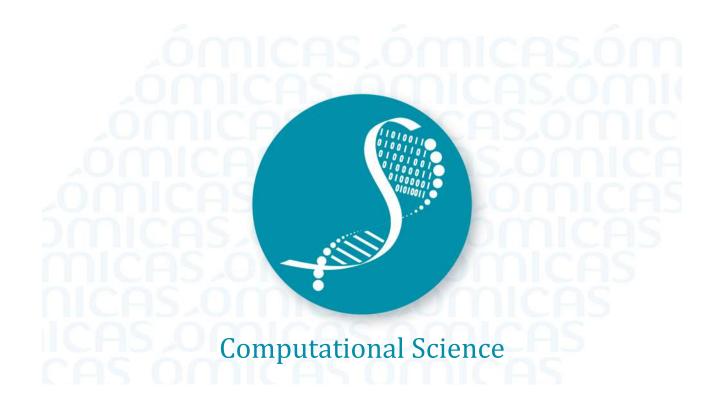


Jaramillo-Botero y Marmolejo, 2019

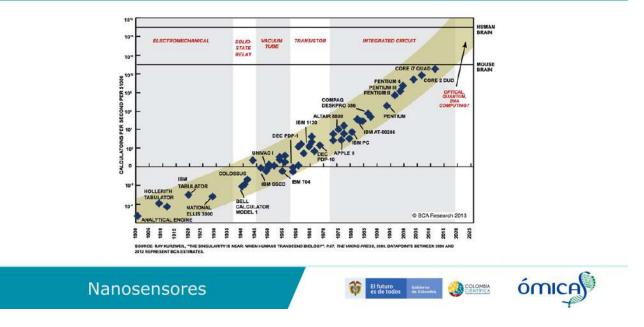








### Computers: Moore's law



### Computational Science: any, and all fields

#### • Computational:

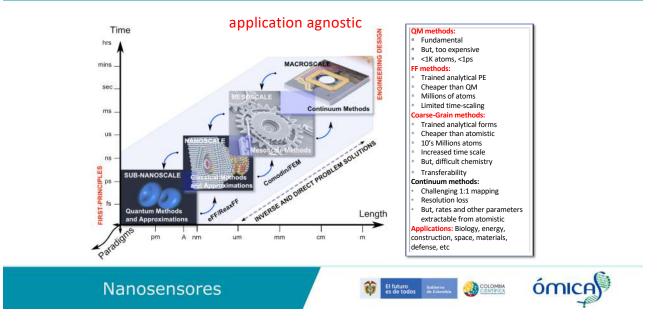
- Physics
- Chemistry
- Biology
- Cosmology
- Climate Modeling
- ... and much more
- We can now simulate:
  - The (almost) exact quantum behavior of a thousand atoms
  - The approximate dynamic behavior of millions of atoms
  - Protein folding geometries during entire folding process
  - 3-dimensional, transient, turbulent reacting combustive flows
  - Global climate with 50 km resolution for next 200 years

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### Theory, methods and tools in computational nanoscience



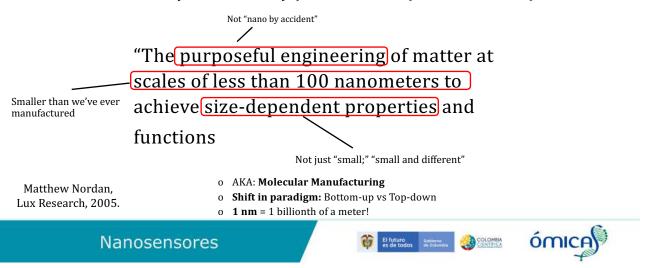
# Why Model from 1st Principles?

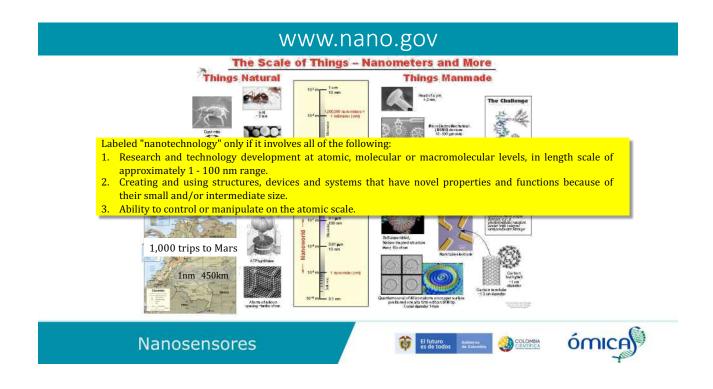
- <u>Access</u> to structural details that are <u>difficult</u> or <u>impossible</u> (e.g. In vivo versus in vitro, etc.) to explore with experiments.
- Enables <u>predictive</u> capabilities (as oppossed to empirical models)
- Also:
- Relatively cheap • Enables evaluation of <u>design</u> alternatives Enables new application development Enables intense analysis of promisory designs (thermodynamical and mechanical) Simulation Reduces time to development improves • Enables development of novel engineering Synthesis development methods at the nanoscale cvcle USC-Caltech (RDX+Al02) Characterization ÓMICA Nanosensores El futuro Bobierne de Colone



# Nanotechnology Definition

"It would be, in principle, possible (I think) for a physicist to synthesize any chemical substance that the chemist writes down.... Put the atoms down where the chemist says, and so you make the substance." - Richard Feynman, *There's Plenty of Room at the Bottom* (Caltech, APS talk, 1959).





### What makes the nanoscale special?

- 1. Interfaces (SA/V)
- 2. Quantum effects
- 3. Thermal fluctuations
- 4. Discreteness of matter

Many material properties, including melting point, fluorescence, surface tension, electrical conductivity, magnetic permeability, and chemical reactivity change as a function of particle size!

### These:

- Can lead to differences between nanosystems and bulk
- Can be exploited to generate whole new devices and phenomena
- Can pose challenges that require novel solutions

Jaramillo-Botero et al, Nanomedicine: A Systems Engineering Approach, Pan Stanford Publishing (World Scientific), Nov. 2008.





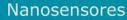
### Surface area (SA) to volume (V)

- A larger SA/V ratio as a function of entity size
  - Assume cube with side l,  $V=l^3$  and  $A=6l^2$  then A/V=6/l increases for small l
  - In cells: surface must allow sufficient exchange to support contents, hence ratio limits size (e.g. Eukaryotic cell  ${\sim}5{-}100\mu m)$
  - Higher ratio leads to more surface available for reactions (e.g. in enzymes)



Jaramillo-Botero et al, Nanomedicine: A Systems Engineering Approach, Pan Stanford Publishing (World Scientific), Nov. 2008.

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• Consider the energy levels of a metal as its size decreases

	large nanoparticle	small nanoparticle
bulk material		

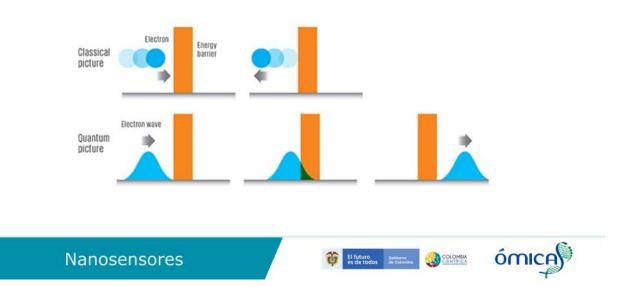
- Heisenberg's Uncertainty Principle: e.g. the more an electron is confined, the greater its momentum range, and vice versa
- Quantum effects can yield a range of exploitable phenomena, e.g.:
  - Nanoscale gold particles selectively accumulate in tumors and the motion of their electrons is confined, which changes its optical response properties, so they can enable both precise imaging and targeted destruction of tumor
  - "Tunability of properties" implies that particle size can be used to fine-tune a material property of interest (e.g., changing fluorescence color in QD)
  - "Electron tunneling" have enabled STMs and flash memories

### Quantized energy states at atomic level

- Discrete quantum levels of a nanocluster may be tuned to modulate the electron transport, normally modulated by the pH, ions, and redox centers.
- Important Quantum effects include "electron tunneling" for STM, quantum Hall effect for resistance calibration instruments, spin polarization in MRI.
- Radiation induced processes such as photoisomerization in vision and photosynthesis in plants depend on quantum yield, which depends in turn on molecular structure.
- Novel optical and magnetic properties for nanometer scale devices potentially, useful for medical diagnosis or intervention.

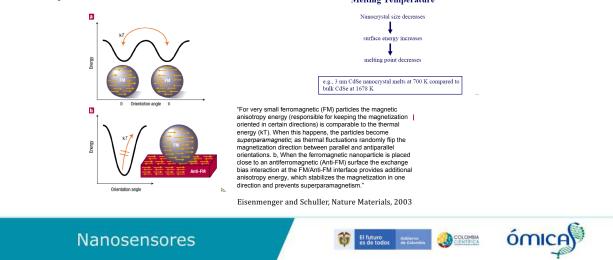


# Quantized energy states at atomic level



### Thermal fluctuations

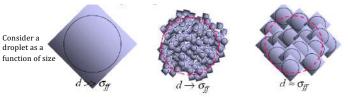
 Thermal fluctuations can be commensurate with size of nanosystem
 Melting Temperature



### Surface Discreteness

Once the size of an entity approaches that of its building blocks:

- Surfaces can no longer be assumed 'smooth' they are ill-defined
  - long alkanes used as lubricants in macrosystems, but act as dirt in nm scale
  - vdW forces in conventional gears taken to the nano hinder normal operation



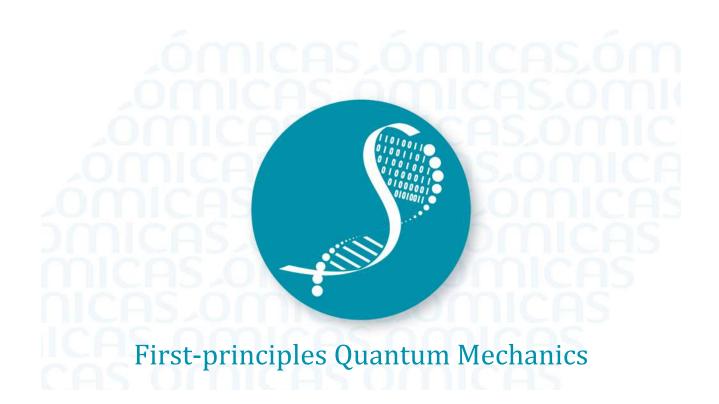
- Thermal fluctuations affect shape and structure
- Obscures bulk concepts as surface tension, dielectric constant, pH

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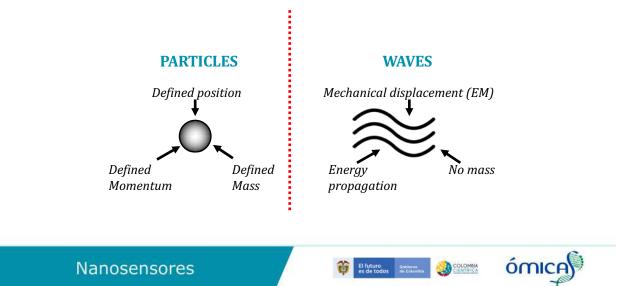
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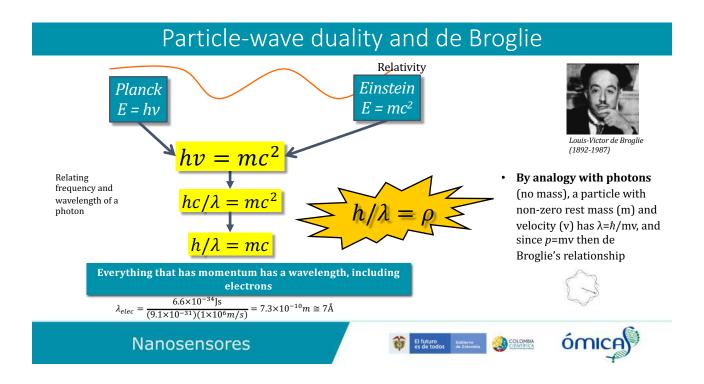
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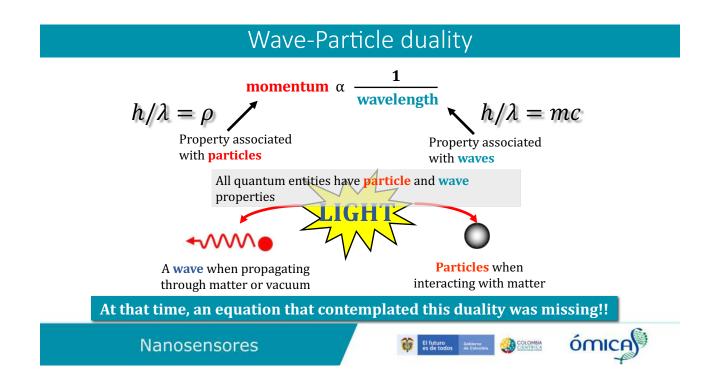
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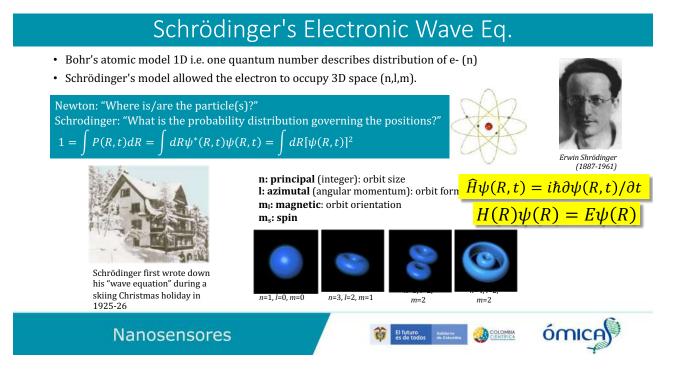


# Diverging physical ideas: <1900

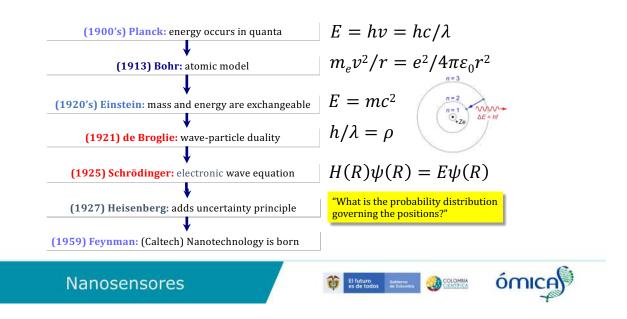


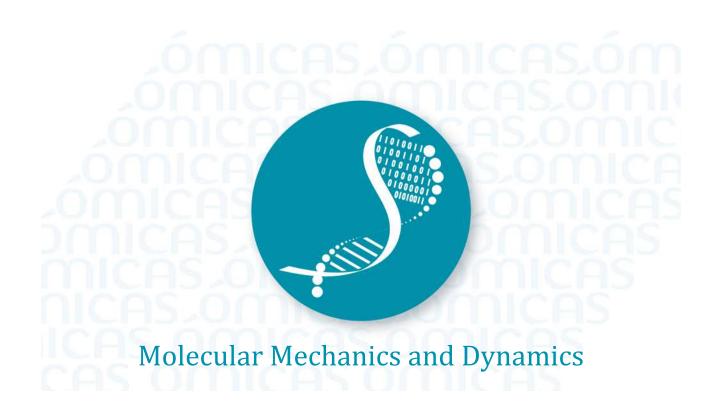






### Historical precedents: summary





### Why avoid the ideal calculation?

Two reasons:

- 1. Too hard or impossible. Exact solutions only exist for a reduced number of cases (H, harmonic oscillator, particle in a box, ...). For systems with a large number of electrons, no analytical solutions have been found (electron-electron repulsion).
- 2. Approximate solutions to the Schrödinger equation can sometimes work well and usually give more "insight" than the exact solutions (e.g. Hückel calculations).

These approximations form the base for what is known today as Molecular Mechanics/Dynamics Simulations.

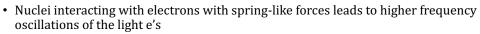
Let's review them.

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### Approximations to Schrödinger's Equation

- 1. Born-Oppenheimer Approximation (1923)
  - aka Adiabatic Approximation
  - Concept:
    - Nuclei are much heavier than electrons (H),
    - Nuclei move in a much slower time scale than electrons.
  - Classical interpretation:



 $M_{nuc} \approx 1.840$ 

#### • Quantum interpretation:

• For the time-dependent Schrödinger's equation we fix the nuclear geometry (at a particular time) and solve the e part of the total wavefunction



# Further Approximations that Lead to MM/MD

- 2. Nuclei moving as classical particles
- Since there are no explicit electronic contributions in the nuclear Schrödinger equation, it can be replaced by a Newtonian EOM
  - Introduces the idea of a Potential Energy Surface (PES)

$$[K_n(R) + V_{nn}(R) + E_{eig}^{el}(R)]\psi^n(R) = E\psi^n(R) \longrightarrow M \frac{\partial^2 R}{\partial t^2} = F \longleftarrow F = -\frac{\partial}{\partial R} \Big[ V_{nn}(R) + E_{eig}^{el}(R) \Big]$$

Nanosensores

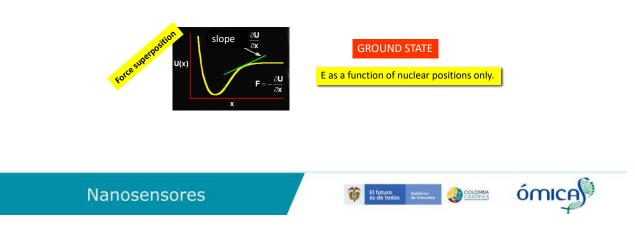
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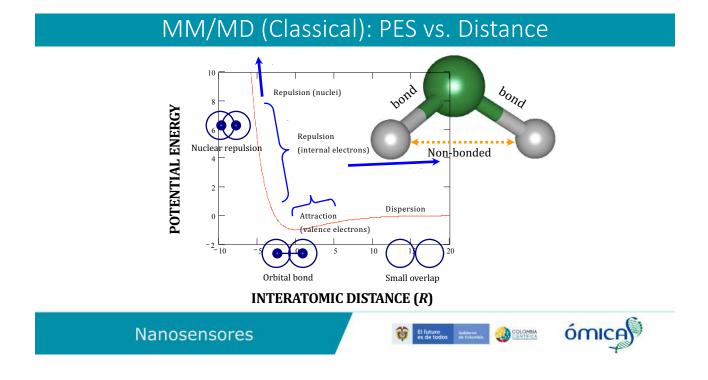
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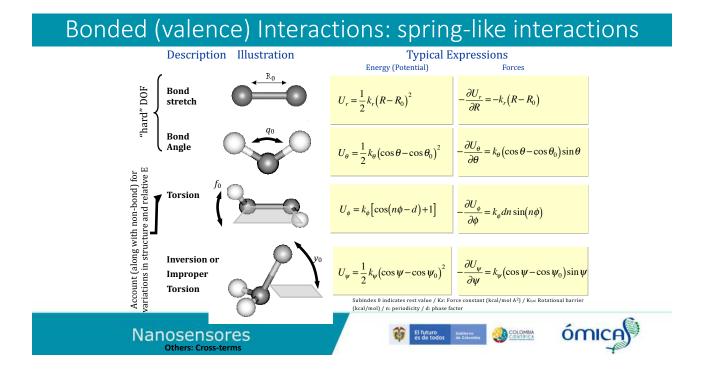
### Further Approximations that Lead to MM/MD

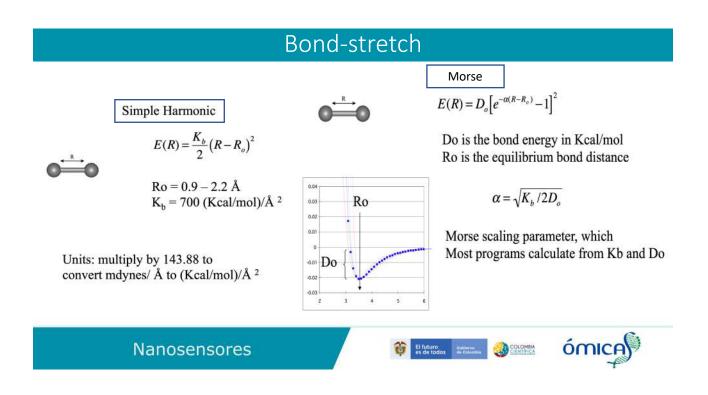
### 3. Approximate PES with analytical potentials

- Avoid solving a Schrödinger equation altogether, and
- ATOMS as classical particles (w/implicit electrons) moving on analytical PES









# Angle bend

Cosine Harmonic



 $E(\theta) = 1/2C[\cos(\theta) - \cos(\theta_o)]^2$ 

Where the force constant is the second Derivative evaluated at the equilibrium angle

$$K_{\theta} = C \sin^2 \theta_{\theta}$$

Input parameters are always in terms of The force constant  $K_{\theta}$  . In general

$$K_q = \frac{\partial^2 E(q)}{\partial q^2} \bigg|_{q=q}$$

Cosine Periodic  $E(\theta) = C [1 - B(-1)^{N} \cos(N\theta)]$ 

This is particularly useful for organometallic systems where N=4 might be used for an Octahedral complex and N=3 might be used for a trigonal center. The parameter B is Either :

 $K_{\theta} = N^2 C$ 

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B = +1 (leading to a minimum for the linear geometry)

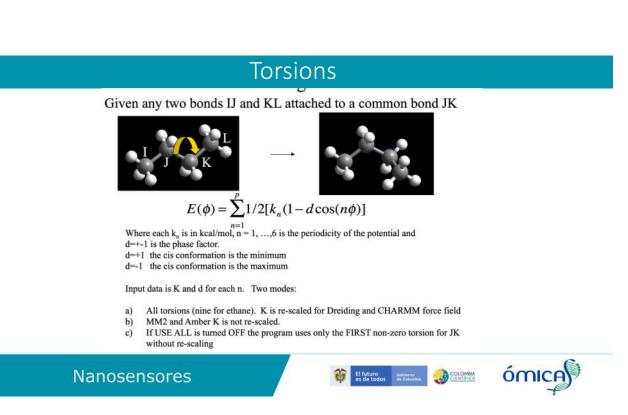
B=-1 (leading to a maximum for the linear geometry)

The periodicity N can be N = 1, 2, 3, ..., 6

The constant C is related to the force constant as

The input is in terms of  $K_ heta$  , N and B

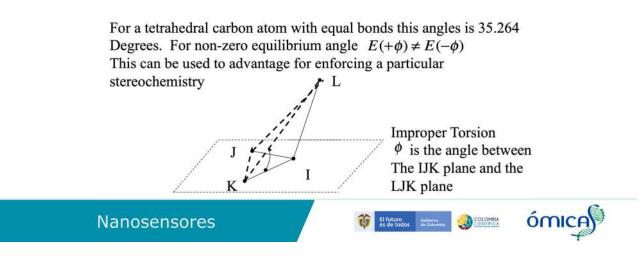
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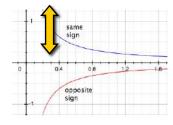
### Improper Torsions

In the CHARMM and Dreiding-I force fields, inversion is defined as if it were a torsion.

 $E(\phi) = 1/2K_{\phi}[\phi - \phi_o]^2$ 



### Non-bond distance-dependent Interactions



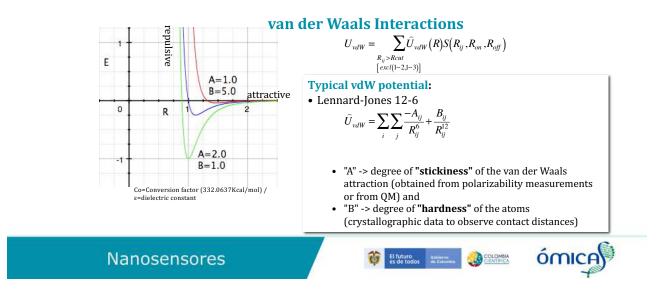
**Electrostatic Interactions**  $U_{Coulomb} = C_0 \sum_{i>j} \frac{Q_i Q_j}{e R_{ij}} S(R_{ij}, R_{on}, R_{off})$ 

A function of charges, interatomic distance, and molecular dielectric (attenuates environment). Partial atomic charges from QM





# Non-bond distance-dependent Interactions



Hydrogen Bonds Conventionally calculated via a pair wise interaction + 3 body angle term

$$E_{HB}(R,q_{AHD}) = E_b(R)E_a(\cos(q_{AHD}))$$

Bond terms:

LJ12-10: 
$$E_{b}(R_{AD}) = AR_{AD}^{-12} - BR_{AD}^{-10} = D_{e}\left[5\left[\frac{R_{e}}{R_{AD}^{-10}}\right]^{12} - 6\left[\frac{R_{e}}{R_{AD}^{-10}}\right]^{10}\right]$$
Morse: 
$$E_{b}(R_{AD}) = D_{e}\left[\chi^{2} - 2\chi\right]$$

$$\chi = e^{-\alpha(R_{AD} - R_{e})} = e^{-\frac{\gamma}{2}\left(\frac{R_{AD}}{R_{e}} - 1\right)}$$
Re is the equilibrium distance between
acceptor (A) and donor (D), A-D, and
$$D_{e}$$
 is the energy well depth.  
Hydrogen bonds:  
• Account for unique water properties  
• hold the 2 strands of DNA double helix together

hold polypeptides together in secondary structures;

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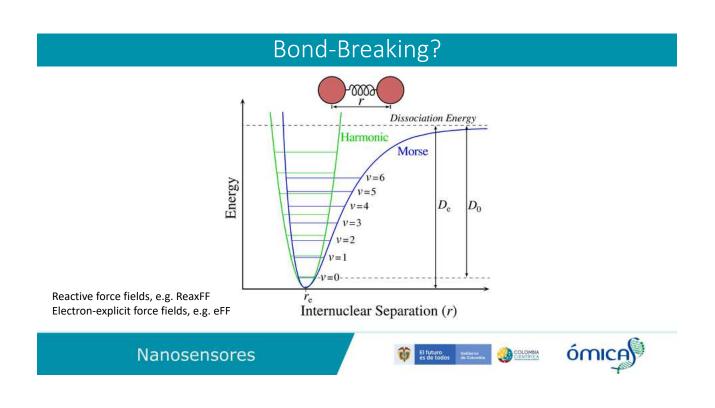
help enzymes bind to their substrate:

help antibodies bind to their antigen help transcription factors bind to each other; help transcription factors bind to DNA

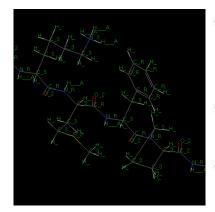
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Angle terms:

$$E_a\left(\cos\left(q_{AHD}\right)\right) = \cos\left(q_{AHD}\right)^4$$



### Atom types



- Atom Type rules make possible the correct assignment of force field parameters throughout the molecule  $K_{\theta_i}, K_n, \theta_o, R_o, D_o$
- The rules are easy for "chemists" to understand and easy to code
- Examples: C\_1, C\_2, C\_3 indicate sp,sp<sup>2</sup>, and sp<sup>3</sup> hybridized carbon atoms

# Conventional and unconventional Force Fields

#### Conventional

- Dreiding (Caltech): J. Phys. Chem. 1990, 94, 26, 8897-8909
- UFF (Caltech): J. Am. Chem. Soc. 1992, 114, 25, 10024-10035
- AMBER (UCSF): Proteins. 2006 Nov 15; 65(3): 712–725
- CHARMM (Harvard): J. Comput. Chem. 4 (2): 187–217, 1983
- MM2: Tetrahedron, Vol 46, Issue 24, 1990, Pages 8005-8018

#### Unconventional

- ReaxFF (Caltech): J. Phys. Chem. A 2001, 105, 41, 9396-9409
- eFF (Caltech): J Comp Chem, 32, 497-512 (2011)
- PQeq (Caltech): J Chem Phys. 2017 Mar 28;146(12):124117.

#### Most Used Molecular Dynamics Codes (open source)

- LAMMPS (lammps.sandia.gov)
- Gromacs (www.gromacs.org)
- NAMD (www.ks.uiuc.edu)

Term	Force Field	Potential
Bonds	Dreiding MM2 AMBER CHARMM	Harmonic Cubic Harmonic Harmonic
Angles	Dreiding MM2 AMBER CHARM	Simple Harmonic MM2 Simple Harmonic Simple Harmonic
Torsions	All	Cosine expansion
Inversions	Dreiding MM2 AMBER CHARMM	Umbreila Not used Improper Torsion JILK Improper Torsion IJKL
Van der Waals	Dreiding MM2 AMBER CHARMM	LJ 12-6 Exp-6 LJ 12-6 LJ 12-6
Off diagonal nonbond	Dreiding MM2 AMBER CHARMM	Combination rule Combination rule except for C- H(exp-6) Combination rule except for H-X of H bonds (LJ 12-10) Combination rule except for H-X of H bonds
Hydrogen bond	Dreiding MM2 AMBER CHARMM	LJ 12-10 Not used Not used LJ 12-10

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Nanosensores

### Summary: From QM to MM/MD

#### Schrodinger equation:

$$H_T \Psi(r, R) = E_T \Psi(r, R)$$
  
where  $H_r = K_r + K_r + V(r, R)$ 

$$H_T = K_n + K_e + V(r, R)$$

Born-Oppenheimer approximation:

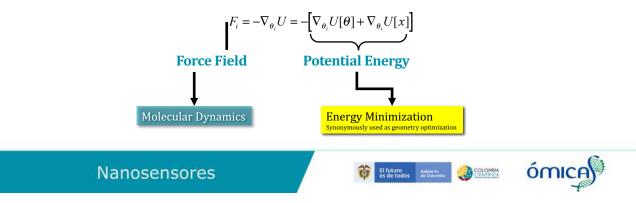
$$\Psi(r,R) = \psi(r,R)\Theta(R)$$

Equation of motion for electrons:

$$(K_e + \nabla)\psi(r, R) = \underbrace{E_e(R)}_e\psi(r, R) \qquad \text{QM}$$
Equation of motion for nuclei (motion on the PES)  
Quantum:  $[K_n + E_e(R)]\Theta(R) = E_T\Theta(R)$   
Classical MD  
(Newtonian Mechanics):  $m\frac{d^2R}{dt^2} = -\nabla E_e(R)$  MM  
Force Field is needed to build up Potential Energy Surface (PES)  
Nanosensores

### QM->PES->FFs->MM/MD

- The Potential Energy depends on the atomic coordinates and the type of bond in accordance with the nature of the element (type of atom), its hybridization state, and other chemical properties.
- Different functional forms of this potential energy lead to the development of different "Force Fields"



### MM: Energy Minimization (EM)

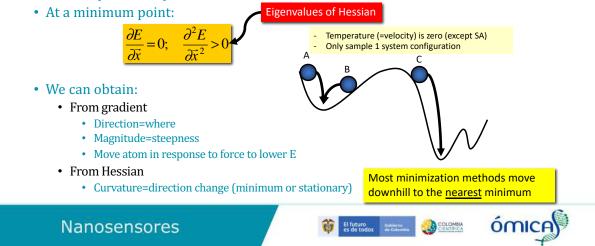
- Purpose: find PE minima in a (hyper) surface
- Why?
  - Minimum points on the PES correspond to stable states (geometries or arrangement of atoms) of the system
- Applications:
  - Geometry optimization (static)
  - Conformation search (for highly populated structures)
  - Study the potential energy surfaces (dynamic)
    - Energy barriers between different conformers or
    - Steepness of a PES around a local minimum
- Keep in mind:
  - Non-trivial systems may have a very large number of minima on the PES (i.e. multidimensional function). Expensive.
  - (Usually) a global minima cannot be analytically guaranteed for non-trivial system (numerical solution) starting from an arbitrary conformation - not necessarily highly populated state



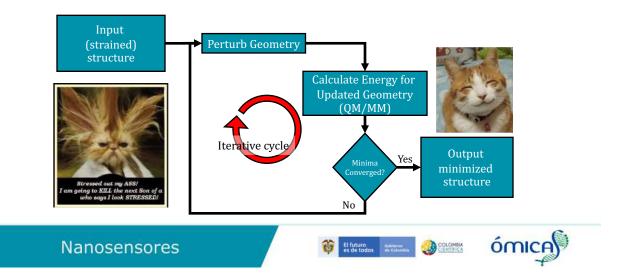
# MM: Energy Minimization (EM)

• The minimization problem in molecular simulations can be stated as:

• Given the QM or MM energy with the Cartesian or internal coordinates of the atoms E(x1,x2,...,xi) -> find the values of all x's where E has a minimum value.



### EM in MD



### Molecular Dynamics: Motivation

- Very similar to physical experiments:
  - Prepare a sample (N particle model)
  - Connect sample to measuring device (computer)
  - Let sample evolve under certain conditions (perform calculations)
  - Measure properties during time interval (equilibrate, then measure)
- An Observable (A): a function of particles position and momenta

$$\mathbf{A}(p^{N}(t),r^{N}(t))$$

- Recall **EM** is used to determine <u>time-independent</u>, <u>temperature-agnostic (velocity=0)</u> minima in the PES, from which one can extract useful properties (limited small systems)
- But, how do we determine a **correct** initial "atomistic" configuration for a system that could compare reasonably to the "macroscopic" ones from experiments, let alone perform dynamics using what we know from MM?



Molecular Dynamics: Motivation• From statistical mechanics (Boltzmann and Gibbs):• Average values are defined as ensemble averages. Replace a single system evolving in  
time with a large number of replications of the system that are considered concurrently,  
i.e.
$$\langle A \rangle_{ensemble} = \int dp^N dr^N \underbrace{A(p^N(t), r^N(t))}_{Polbability density} P(p^N, r^N) \\ Polbability density P(p^N, r^N) \\ Polbability P(p^N,$$

### When to use EM and when to use MD?

#### Recall, we can use MM-EM:

- To determine stable configuration states of a single system.
- To determine 0K properties of a single system configuration.
- To calculate normal modes and vibrational modes of a system.
- To calculate relative energies and transition states/structures.
- To calculate IR-spectra, IV or NMR-spectra.
- To compute single-component system properties ...

#### MD:

- To sample the conformational space of a system at T>0K.
- To model temperature and pressure effects.
- To obtain thermodynamics and time-dependent (kinetic) properties.
- To compute multi-component system properties ...

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### **MD:** Applications

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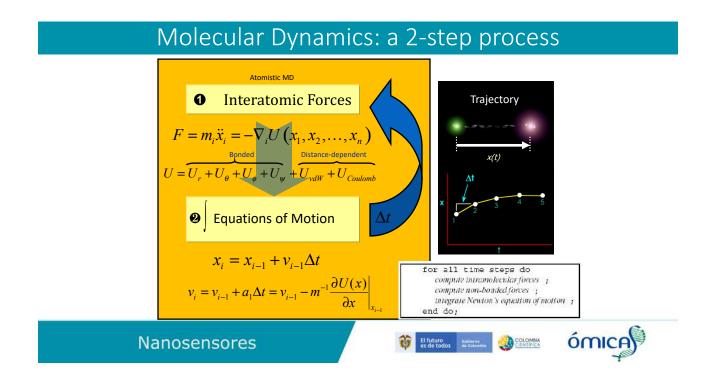
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- Liquids: phase transitions, viscosity, heat flow, multicomponents
- Defects: propagation, interstitials, grains, dislocations (point-linear-planar)
- Fracture: propagation, initiation, evolution, speed
- Surfaces: roughness, diffusion, melting, faceting
- Friction: tribology, adhesion
- Clusters: melting, role of surface and anisotropy, catalysis
- Spectra: scattering
- Biomolecules: protein, nucleic acids, membranes conformation, free energy, surface free energy
- **Transport properties:** phase transitions, phonons, thermoelectrics
- Non-equilibrium phenomena: plasmas, combustion, turbulent flow,...
- Limitations ...
  - Transferability
  - As good as the force field
    Light atoms (not He, Ne, H<sub>2</sub>)
  - No excited states
  - Time (e.g. enough to reach equilibrium or detect infrequent events, i.e. longer than relaxation time of quantities of interest)

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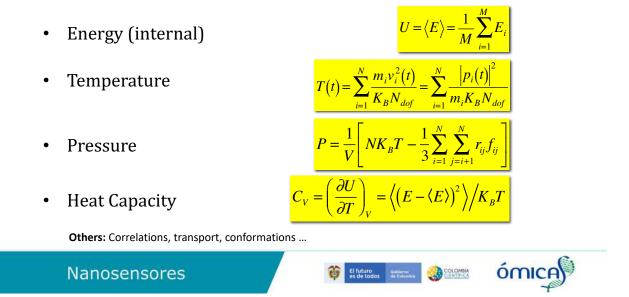
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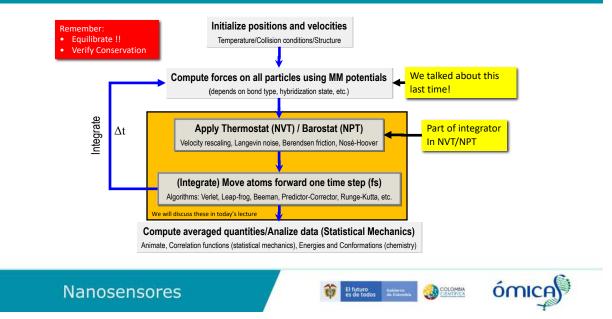
Simulation Ensembles		
IF	GIVES	
nVE=constant:	• <b>Microcanonical ensemble</b> . Total energy and volume controlled. Free run, no velocity or pressure scaling. Requires PBC for solvated simulations.	
nVT=constant:	• <b>Canonical ensemble.</b> T controlled through random perturbations on atoms per step to simulate interaction with a heat bath [Andersen, 1980], velocity rescaling to maintain kinetic temperature, or adding friction terms.	
nPT=constant:	• <b>Isobaric ensemble.</b> P controlled via changes in system volume to match desired pressure (scale positions and boundaries by factor).	
(μ)VT=constant:	<ul> <li>Grand-canonical ensemble. N is allowed to fluctuate. Closely represents experimental conditions, gives direct access to the equation of state.</li> </ul>	
Jaramillo-Botero y Mamolejo 2019.07CS n=number of particles; V=Volume; E=Energy; T=Temperature; P=Pressure, µ=chemical potential		

#### Ensembles System: Heat bath: T Heat bath: $T,\mu$ t dE dEN, V, EdNSystem: System: N, V, T V, T, µ Microcanonical: completely isolated Canonical: System in contact with a Grand Canonical: In contact with a heat heat bath of temperature T, energy bath of temperature T and particle bath exchange but no particle exchange of chemical potential $\mu$ : energy and particle exchange ÓMICA Nanosensores Jaramillo-Botero y Marmolejo 2019 nuro COLOMBIA

# Important Properties of Interest



# MD Flowchart (ensembles)

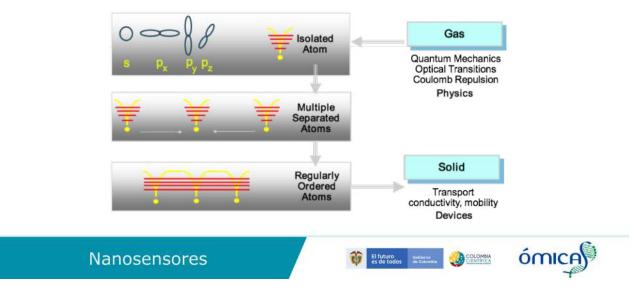




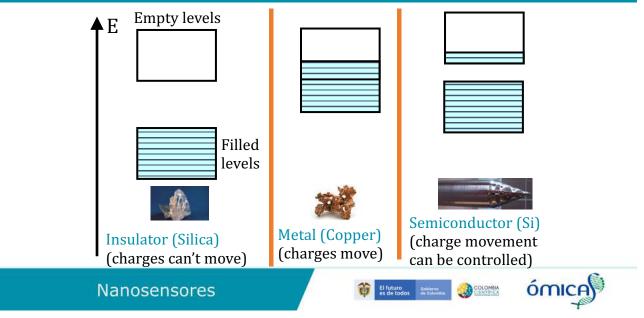
**Electronic Transport Properties in the Nanoscale** 

#### Electron Conduction in Solids

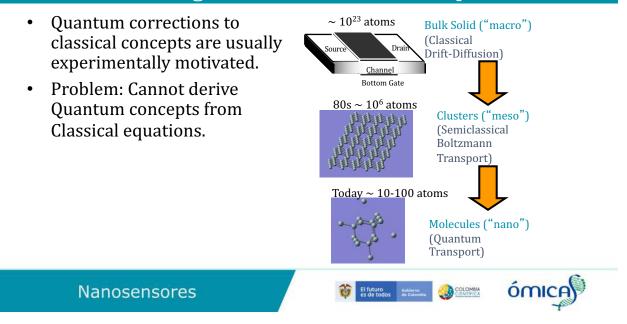
• Bands are channels in which electrons move "freely".



# Filling up the Bands with Electrons



# Pushing the simulation envelope

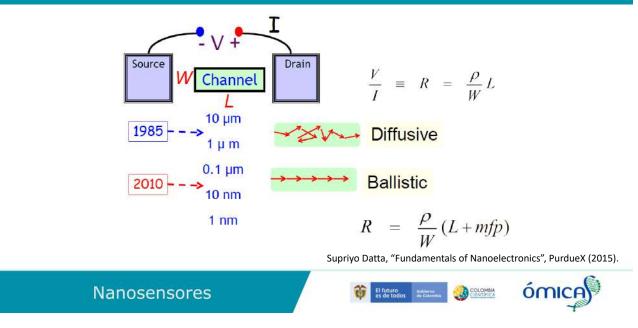


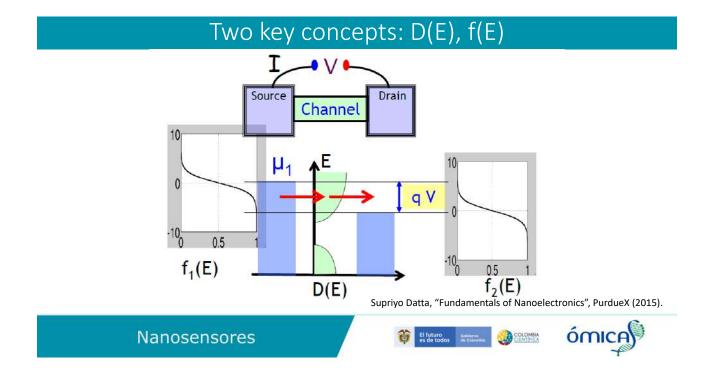
#### Determining the Most Appropriate Model

• Length Scales and Interactions Determine the Most Appropriate Model.

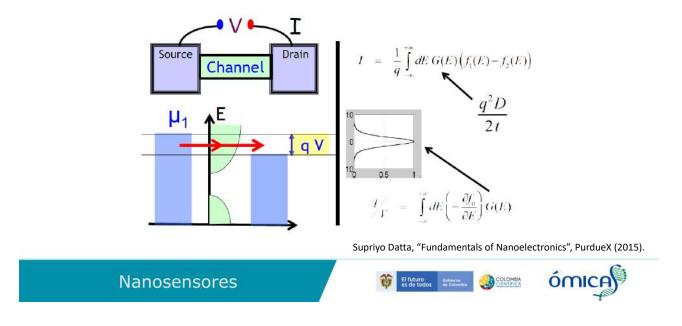
Transport Regime	Quantum	L < l <sub>e-e</sub> Ballistic	$L >> l_{e-e}$ Fluid	Fluid	Diffusive
1.54	<u></u>				
Scattering	Rare	Rare	e-e (Many), e-	ph (Few)	Many
Model:					
Drift-Diffusion					
Hydrodynamic	Quantum H	lydrodynamic			
Monte Carlo			l <mark>.</mark>		
Schrodinger/Green's					
Functions	Wave	1			
		D. IV. d.	Ĩ.	î/	
Applications	Nanowires,	Ballistic			
	Superlattices	Transistor	Current IC's	Current IC's	Older IC's

# Change in paradigm





# Why electrons flow



#### Quantum Transport far from Equilibrium Macroscopic dimensions Non-Equilibrium Quantum Statistical Mechanics Diffusive Ballistic Quantum Atomic dimensions Drift / Diffusion Boltzmann Transport $\mu_{l}$ Цŋ led Non-Equilibrium **Green Functions** WHERE AN S D SILICON $= V_{a}$ $\pm v_p$ - 1 - 1 Supriyo Datta, "Fundamentals of Nanoelectronics", PurdueX (2015). ÓMICA Nanosensores El futuro es de todos Û

# Non-Equilibrium Green's Functions (NEGF)

- Most fundamental and accurate method.
- Considered by many to be the most difficult quantum approach.
- Formulation of scattering rather straightforward and theoretically sound including incoherence and irreversibility.
- Implementation of scattering rather difficult.
- Computationally intensive.



Non-Equilibrium Green's Functions (NEGF)

$$f_{1} [\Sigma_{1}] [\Sigma_{2}] f_{2}$$

$$\Sigma = \Sigma_{1} + \Sigma_{2}$$

$$\Gamma = \Gamma_{1} + \Gamma_{2}$$

$$\Sigma^{in} = f_{1}\Gamma_{1} + f_{2}\Gamma_{2}$$

$$\Gamma_{1,2} = i[\Sigma_{1,2} - \Sigma_{1,2}^{+}]$$

(1) Green's function  $G^{R} = [EI - H - \Sigma]^{-1}$ (2) "Electron density"  $G^{n} = G^{R} \Sigma^{in} G^{A}$ (3) "Density of states"  $A = G^{R} \Gamma G^{A} = G^{A} \Gamma G^{R}$   $= i[G^{R} - G^{A}]$ (4) Current per unit energy at terminal 'p'

$$\tilde{I}_p = -\frac{q}{h} Trace [\Sigma_p^{in} A - \Gamma_p G^n]$$

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Supriyo Datta, "Fundamentals of Nanoelectronics", PurdueX (2015).

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# Generalities

- A biosensor is an analytical device, used for the detection of a chemical substance, that combines a biological component with a physicochemical detector.
- The transducer or the detector element, which transforms one signal into another one, works in a physicochemical way, resulting from the interaction of the analyte with the biological element, to easily measure and quantify.

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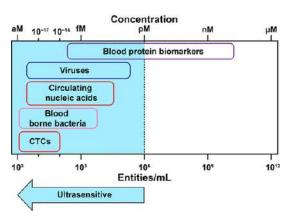
#### Biotransducer

- Biosensors can be classified by their biotransducer type.
- The most common types of biotransducers used in biosensors are:
  - Electrochemical biosensors
  - Optical biosensors
  - Electronic biosensors
  - Piezoelectric biosensors
  - Gravimetric biosensors
  - Pyroelectric biosensors



#### Opportunities

- There are many opportunities in the sensing field for detecting and measuring very low analyte concentrations.
  - Sub-picomolar detection limits represent useful concentration ranges for the detection of many disease biomarkers.



Yanfang Wu, Richard D. Tilley and J. Justin Gooding, J. Am. Chem. Soc. 2019, 141, 3, 1162-1170



### Challenges

- Achieving sub-picomolar detection limits has three major challenges:
  - 1. Assay sensitivity
    - One strategy to gain greater sensitivity involves confining the sensing volume to the nanoscale, as used in nanopore- or nanoparticle- based sensors
  - 2. Response time
    - Methods to improve response time typically focus on obtaining an intimate mixture between the sensor and the sample either by extending the length scale of nanoscale sensors using nanostructuring or by dispersing magnetic nanoparticles through the sample to capture the analyte

#### 3. Selectivity (including limiting background signals).

• One solution to help address the challenge of selectivity is loading nanoparticles with many biorecognition species is

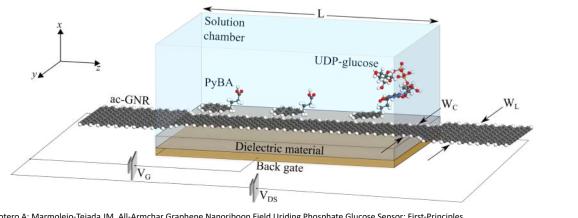
Yanfang Wu, Richard D. Tilley and J. Justin Gooding, J. Am. Chem. Soc. 2019, 141, 3, 1162-1170

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# UDP-glucose sensor



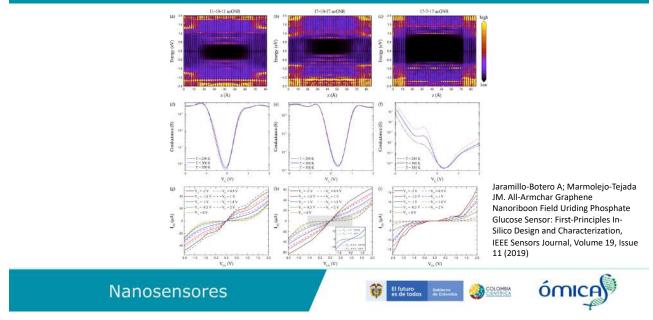
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Jaramillo-Botero A; Marmolejo-Tejada JM. All-Armchar Graphene Nanoriboon Field Uriding Phosphate Glucose Sensor: First-Principles In-Silico Design and Characterization, IEEE Sensors Journal, Volume 19, Issue 11 (2019)

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# UDP-glucose sensor

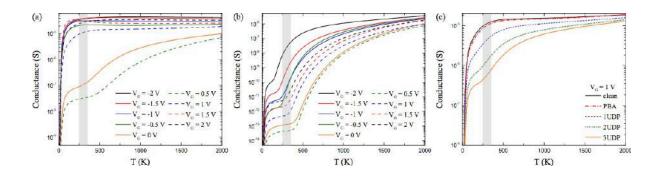






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# UDP-glucose sensor



Jaramillo-Botero A; Marmolejo-Tejada JM. All-Armchar Graphene Nanoriboon Field Uriding Phosphate Glucose Sensor: First-Principles In-Silico Design and Characterization, IEEE Sensors Journal, Volume 19, Issue 11 (2019)

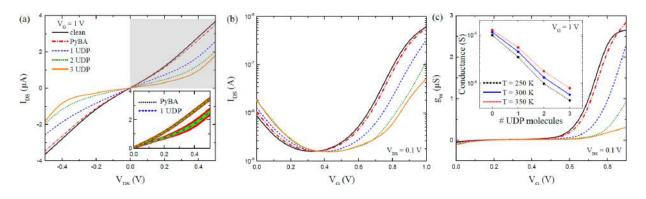




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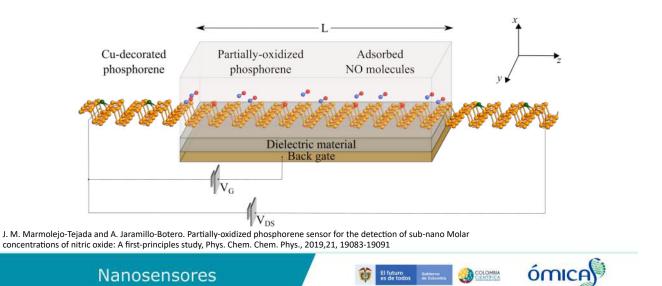
# UDP-glucose sensor

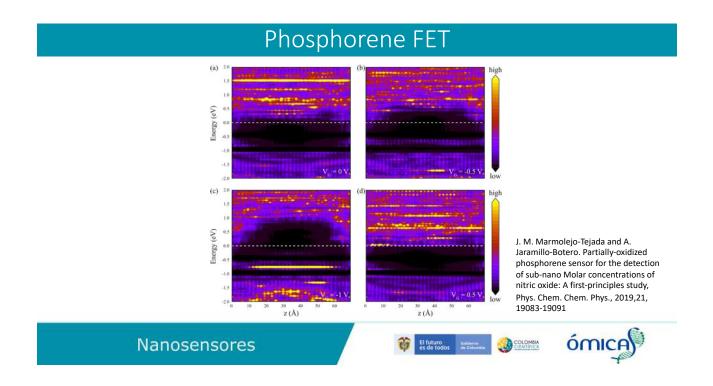


Jaramillo-Botero A; Marmolejo-Tejada JM. All-Armchar Graphene Nanoriboon Field Uriding Phosphate Glucose Sensor: First-Principles In-Silico Design and Characterization, IEEE Sensors Journal, Volume 19, Issue 11 (2019)

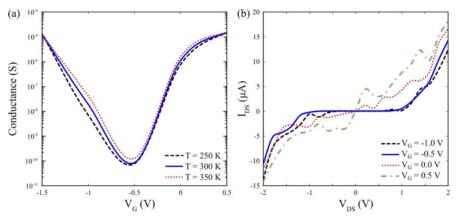


# Volatile organic compounds (VOCs) sensor





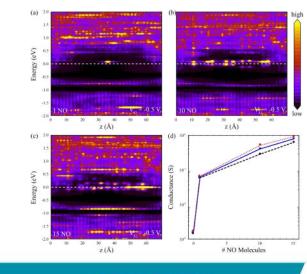
# Phosphorene FET

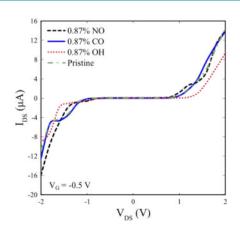


J. M. Marmolejo-Tejada and A. Jaramillo-Botero. Partially-oxidized phosphorene sensor for the detection of sub-nano Molar concentrations of nitric oxide: A first-principles study, Phys. Chem. Chem. Phys., 2019,21, 19083-19091

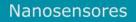


# Nitric Oxide (NO) sensor

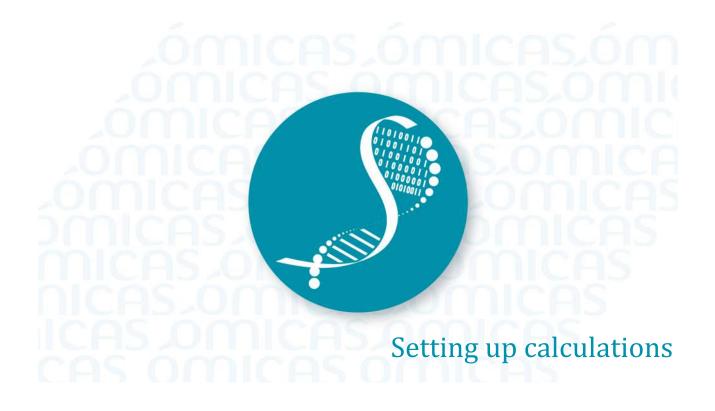


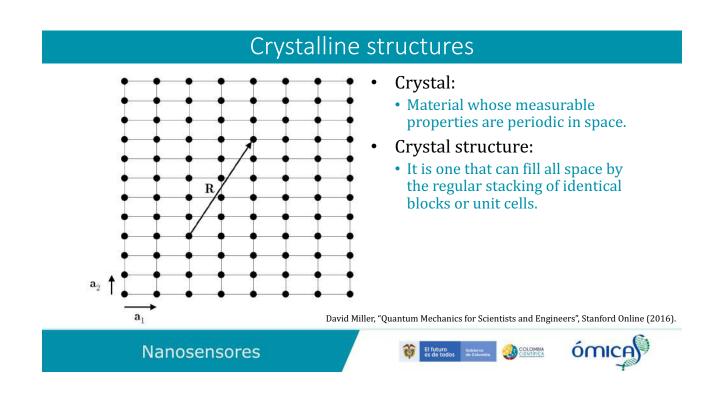


J. M. Marmolejo-Tejada and A. Jaramillo-Botero. Partially-oxidized phosphorene sensor for the detection of sub-nano Molar concentrations of nitric oxide: A first-principles study, Phys. Chem. Chem. Phys., 2019,21, 19083-19091



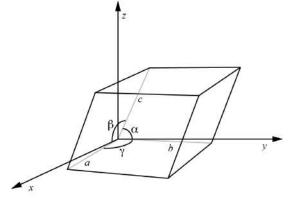






#### Crystalline Systems

- Unit cell:
  - Smallest repetitive volume which contains the complete lattice pattern of a crystal.
  - *a*, *b* and *c* are the edge lengths.
  - $\alpha$ ,  $\beta$  and  $\gamma$  are interaxial angles.



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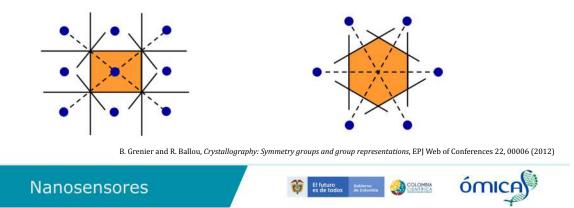
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# Provide the second state physics • The reciprocal lattice is defined as a network of points in the Fourier space: • $\vec{\tau} = h\vec{a}^* + k\vec{b}^* + l\vec{c}^*$ • with h,k,l integers and $\vec{a}^*, \vec{b}^*, \vec{c}^*$ the basis vectors of the reciprocal lattice: • $\vec{a}^* = C \frac{\vec{b} \times \vec{c}}{V}, \vec{b}^* = C \frac{\vec{c} \times \vec{a}}{V}, \vec{c}^* = C \frac{\vec{a} \times \vec{b}}{V},$ • with C a constant and V the volume of the unit cell in direct space: • $C = \begin{cases} 2\pi & \text{in solid state physics} \\ 1 & \text{in crystallography} \end{cases}$ • $V = (\vec{a} \times \vec{b}) \cdot \vec{c} = \vec{a} \cdot (\vec{b} \times \vec{c})$

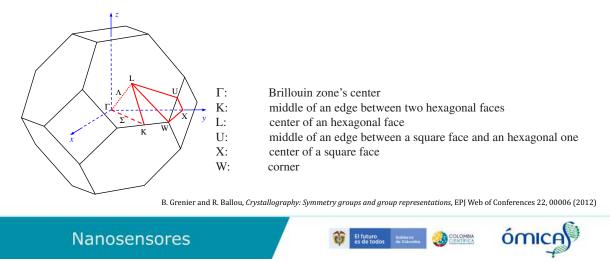
# The Brillouin zone

- Smallest polyhedron enclosed by the perpendicular bisectors of the nearest neighbors to a given point of the reciprocal space.
- First Brillouin zone for the two-dimensional rectangular and two-dimensional hexagonal reciprocal lattices:



#### The Brillouin zone

• First Brillouin zone for a three dimensional cubic F reciprocal lattice.





- The band structure of a material determines its electronic and optical properties.
- Band structure calculations require solving the Schrödinger equation using particle wave functions in a periodic potential:
  - $\psi_{nk}(r) = \exp(ikr)u_{nk}(r)$
  - where  $\psi(r)$  is an eigenfunction of the system and is defined as the product of a plane wave envelope and a periodic Bloch function u(r); ncorresponds to the band index, while k corresponds to the wave vector associated with the direction of motion of the electron in the crystal and takes on values within the corresponding Brillouin zone.
- The band structure is determined by the orbital energies  $\varepsilon_{nk}$  for each band *n* and momentum *k*.

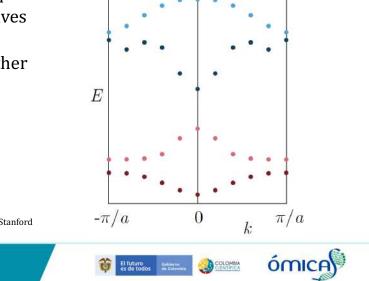
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# Band structure diagrams

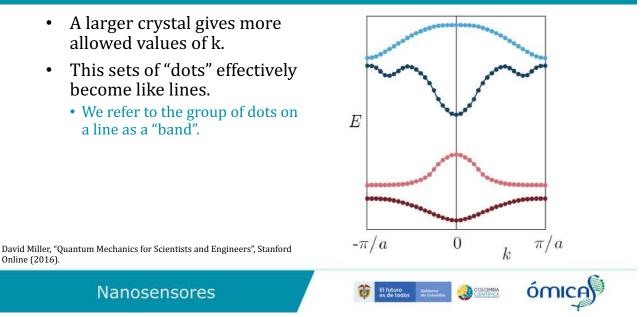
- Solving the one-electron Schrödinger equation gives energy eigensolutions.
- We continue with the other allowed values of k.



David Miller, "Quantum Mechanics for Scientists and Engineers", Stanford Online (2016).

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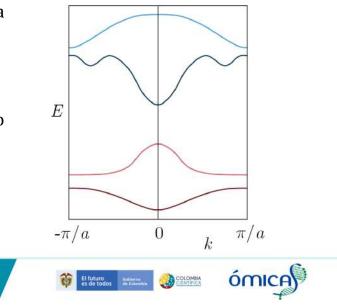
### Band structure diagrams



#### Band structure diagrams

- There are multiple bands in a band structure, in fact, an infinite number, but usually only a few are important for the properties of a material.
- In each band, we only have to plot k-values from  $-\pi/a$  to  $\pi/a$ .
- This range is known as the (first) Brillouin zone.

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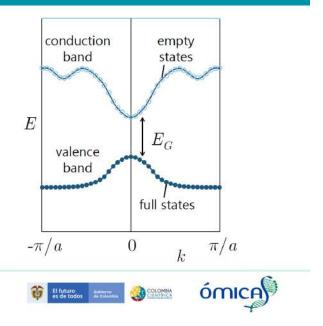
#### Semiconductors and insulators

 Semiconductors and insulators have an (almost) completely full band (the valence band) separated by a "bandgap" of energy *E<sub>G</sub>* from an (almost) completely empty band (the conduction band).

David Miller, "Quantum Mechanics for Scientists and Engineers", Stanford

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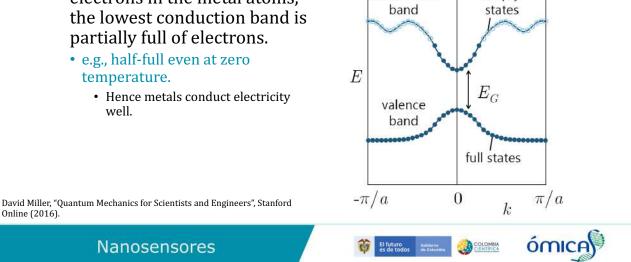
Online (2016).



David Miller, "Quantum Mechanics for Scientists and Engineers", Stanford Online (2016).

#### Metals

Because of the number of • electrons in the metal atoms, the lowest conduction band is partially full of electrons.



conduction

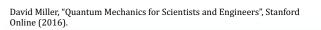
empty

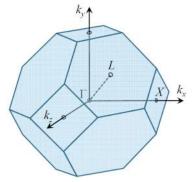
#### Brillouin zone in 3D

• The Brillouin zone for the diamond or zinc-blende lattice is a 3D object.

Online (2016).

- Two important directions are:
  - *X*: Along one of the coordinate directions.
  - *L*: Along one of the cube space diagonals.
- The center is the  $\Gamma$  (gamma) point.





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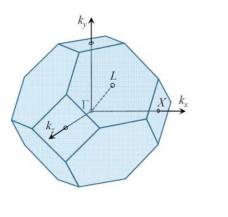
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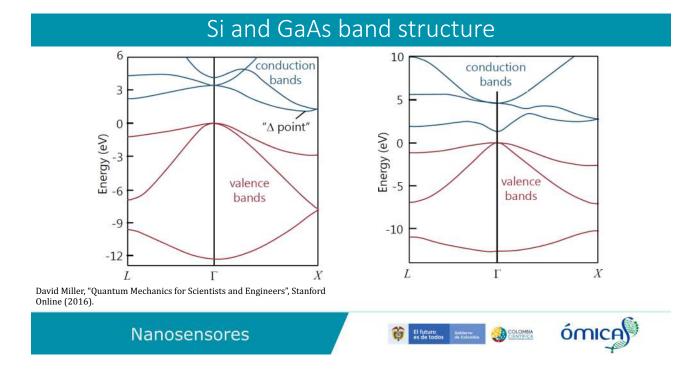
# Brillouin zone in 3D

- Typically, the band structure is calculated only along a few directions.
  - Such as along the lines from the Γ point (at the center of the Brillouin zone) to the X point and the L point.



David Miller, "Quantum Mechanics for Scientists and Engineers", Stanford Online (2016).







### DFT calculations with Quantum ESPRESSO

- We will begin our test calculations using the online tool: <u>https://nanohub.org/tools/dftqe</u>
- This tool allows us to run quantum ESPRESSO (a powerful electronic structure code based on density-functional theory, plane waves, and pseudopotentials) for performing several calculations:
  - Total energy.
  - Energy minimization to predict structures.
  - Kohn-Sham band structure of periodic systems and phonons.
  - Cell and force relaxation.
  - Output of Stress and forces.

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#### Silicon Band Structure

Premade atomistic structure	Si diamond	
Atomic Coordinate	Fractional	
	cubic F (tcc)	
	Silicon band structure	
Atomic Shuchan	2 Silicon disamud structure Si 0.0 0.0 0 Si 0.25 0.25 0.25	
	-3 715 5 715 8 000 -5 715 0 000 5 715 0 000 2 716 2 715	
Latice Parameter "a" (A	5.43	1.1.
Ratio Lattice Parameters "tv/a	1	A
	1	12

• The tool already has some premade atomistic structures with their corresponding cell parameters and atom coordinates.

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• Choose Si diamond.

 
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### Silicon Band Structure

input Geometry Energy Expression	Phonomy   Band Structure/DO	S Advanced Options	
Exchange and Constation functional	10.0.24		203
Hatay	No		
California Security and			
X direction: 8			1.A.1
V direction			- A.I.
Z direction 8			LA.
and a second			
Number of bands	0		1.1.
Wavefunction Kinetic Energy cutoff (Ry)	16.0		.A.
Charge Density Kinetic Energy cutoff (Ry):	96.0		LA.I
SCF Convergence Criterion (Ry)	16-6		-A.I.
SCF maximum steps:	100		+ -
Enable accupation options	· j= yes		
Anna Internation			- 1 M

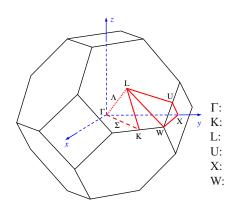
- We can choose LDA or GGA functionals and enable/disable relaxation.
  - Choose GGA and no relaxation, but you should also explore the other options.
- Specify k-points in the reciprocal space, as well as other calculation parameters.
  - We will use default values for the moment.



# Silicon Band Structure

Christianistics with Countains ESPRESSO         Christ       Christianistics         Participanistic       Christianistics         Participanistics       Christianistics	<ul> <li>Enable Band Structure Calculation, choose the path along the high-symmetry points you wish to explore and the number of k-points along the path.</li> <li>Notice your path goes from L(0.5, 0.5, 0.5) to Γ(0.0, 0.0, 0.0) to X(1.0, 0.0, 0.0).</li> </ul>
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Remember the 1<sup>st</sup> Brillouin zone for a 3D cubic reciprocal lattice



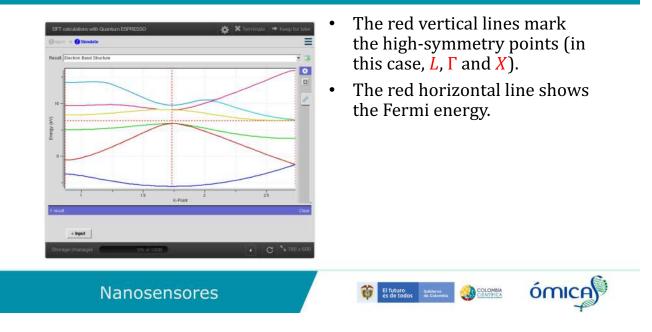
Brillouin zone's center middle of an edge between two hexagonal faces center of an hexagonal face middle of an edge between a square face and an hexagonal one center of a square face

corner

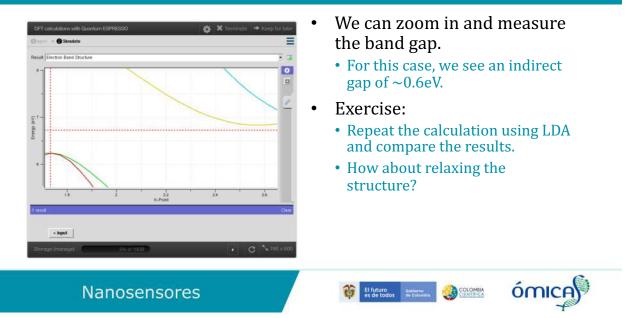




### Silicon Band Structure



## Silicon Band Structure



#### Input scripts

CPT cadodations with Chandram EXPRESSIO     * Control       Control     Control	<ul> <li>So far, we have not discussed the particularities of our input script, but you should study all the input scripts necessary for this calculation and get familiar with their structure and format.</li> <li>Fore more details on each command, check the input file description help at: <u>https://www.quantum- espresso.org/Doc/INPUT_PW.ht</u> <u>ml</u></li> </ul>
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# GNR Band Structure

- Let's continue using the nanohub's online tool for calculating the band structure of a GNR.
- This time, we will import the coordinates and type in the cell parameters.
  - Check the provided xyz file, which was created with Nanoribbon tool in QuantumATK.

14			
_a 20	)_b 20 _c 4.2	6258 _alph 9	0 _beta 90 _gamm 90
С	5.00000	5.00000	2.84172
С	5.00000	6.23050	3.55215
С	5.00000	5.00000	1.42086
С	5.00000	7.46100	2.84172
С	5.00000	8.69150	3.55215
С	5.00000	6.23050	0.71043
С	5.00000	7.46100	1.42086
С	5.00000	9.92200	2.84172
С	5.00000	8.69150	0.71043
С	5.00000	9.92200	1.42086
Н	5.00000	4.05603	3.38672
Н	5.00000	4.05603	0.87586
Н	5.00000	10.86597	3.38672
Н	5.00000	10.86597	0.87586

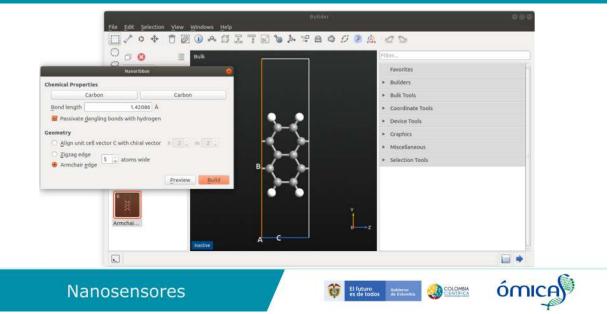




# QuantumATK's Nanoribbon tool



# QuantumATK's Nanoribbon tool



Characteristics	50	fthe	xyz fi	le
<ul> <li>The first line indicates the number of atoms, n.</li> <li>Second line is a comment.</li> <li>In this case, we included the cell dimmensions and angles.</li> <li>Notice the structure is periodic on the z-direction.</li> </ul>	14 _a 2 C C C C C C C C C	0 _b 20 _c 4.2 5.00000 5.00000 5.00000 5.00000 5.00000 5.00000 5.00000 5.00000	26258_alph 9 5.00000 6.23050 5.00000 7.46100 8.69150 6.23050 7.46100 9.92200	00 _beta 90 _gamm 90 2.84172 3.55215 1.42086 2.84172 3.55215 0.71043 1.42086 2.84172
• The following <i>n</i> lines contain the element symbol and corresponding position vector in Angstroms.	C H H H	5.00000 5.00000 5.00000 5.00000 5.00000 5.00000	8.69150 9.92200 4.05603 4.05603 10.86597 10.86597	0.71043 1.42086 3.38672 0.87586 3.38672 0.87586

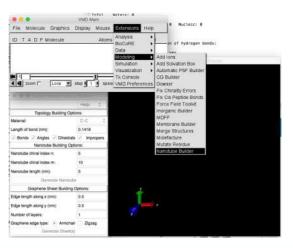
Nanosensores

El futuro solitimos de Colombia



# VMD's Carbon Nanostructure Builder Tool

• Note we can also use open source tools, such as VMD, for getting the system's coordinates.

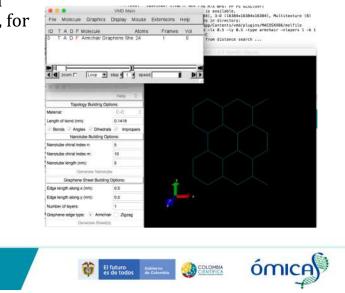






# VMD's Carbon Nanostructure Builder Tool

 Note we can also use open source tools, such as VMD, for getting the system's coordinates.



Nanosensores

# **GNR Band Structure**

htput - O tandata htput Geometry ) Energy Exp Premade atomics structure [up	pression   Phonons   Bant ShuchareDOS   Advanced Options   Insided data	<ul> <li>system in xyz format.</li> <li>The provided file has positions in Angstroms, then you should</li> </ul>
	Cartesian Extension uniticell (free) SAGNR band shuctare	select Cartesian Atomic Coordinates.
Atonic Structure	14 c 5.00000 5.00000 2.94172 c 5.00000 4.2050 3.55215 c 5.00000 5.00000 1.42065 c 5.00000 7.46100 1.84172 20.00 0.000 0.000	Select free type of unit cell
	0,000 20,00 0,000 0,000 0,000 4,263 20.0 1	and fill up the Cell Vectors in Angstroms.
		Terrelatio >
Slange (mirtige)	gių at tradit 💽	C ** 760 x 600
N	anosensores	

## **GNR Band Structure**

Exchange and Correlation functional GGA Fielded No X direction V direction 2 direction 100	
Synta Halana (Selanosa Segura) X disector (	
X desction 1 V desction 1	
Y direction 1	
	-
Z direction 100	
	- 171
Number of Isends 44	LAD
Wavefunction Famelic Energy cutoff (Ry) 16.0	
Charge Density Kinetic Energy cutoff (Ry) 96.0	
SCF Convergence Criterion (Ry). 1E-6	- 71
SCF maximum sheps 100	+ -
Enable occupation options: 💗 🏐 m yes	Contraction of the local division of the loc
Archightune Ophanel	

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- Since the GNR is only periodic on the z-direction, we only increase the number of kpoints on that direction.
  - The number of k-points in the other directions is set to 1.
- Type in the number of bands.

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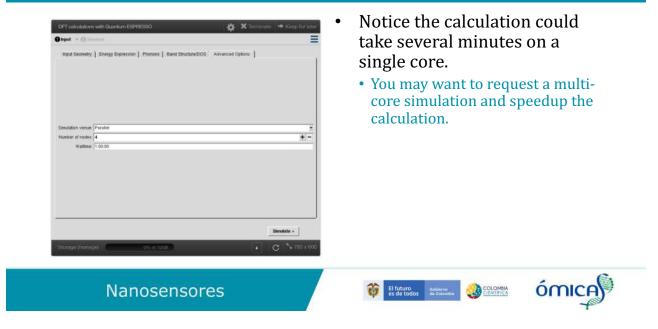
• Remember carbon has 4 Valence electrons and hydrogen just 1.

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# **GNR Band Structure**

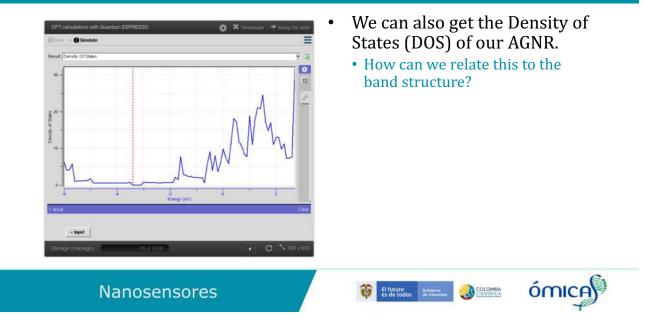
Def calculations with Quantum ESPRESSO         Paper         Paper	<ul> <li>We are interested in computing the band structure along the transport direction (z-direction).</li> <li>Then, the path goes from Z(0.0, 0.0, 0.5) to Γ(0.0, 0.0, 0.0) to Z(0.0, 0.0, 0.5).</li> </ul>
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# **GNR Band Structure**



#### **GNR Band Structure** We can zoom in around the • 4 × 10 Fermi energy and measure Ξ . the bandgap of our AGNR. 0 • In this case, we get a direct gap 0 of ~0.35eV. Real P « Nput ÓMICA 😻 El futuro Enbierne 🕹 Colombia Nanosensores

# GNR Density of States



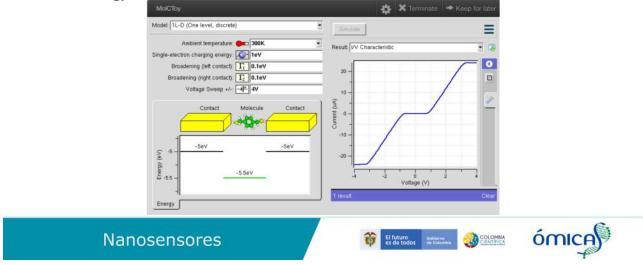
# Electrical Conduction through a molecule

- We can also use nanohub's tools for computing electrical conduction through a molecule: <u>https://nanohub.org/resources/molctoy</u>
- This tool computes current-voltage (I-V) characteristics and conductance spectrum (G-V) of a molecule sandwiched between two metallic contacts.



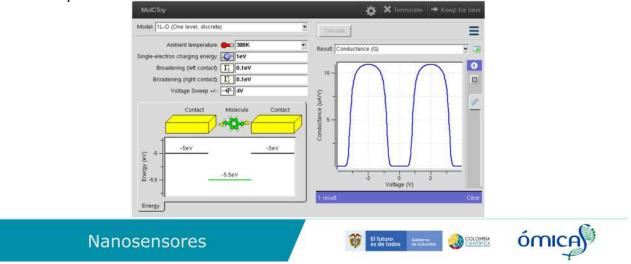
# Electrical Conduction through a molecule

• The 1 level discrete model represents a molecule with a single energy level.



# Electrical Conduction through a molecule

• After running our calculation, we can observe Conductance and I/V characteristics .



# Electrical Conduction through a molecule

• What happens when 2 energy levels are considered?

